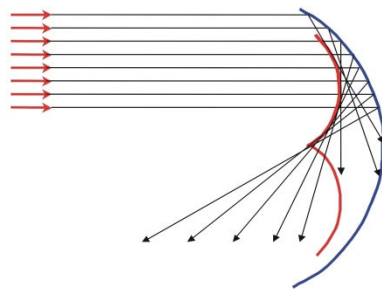
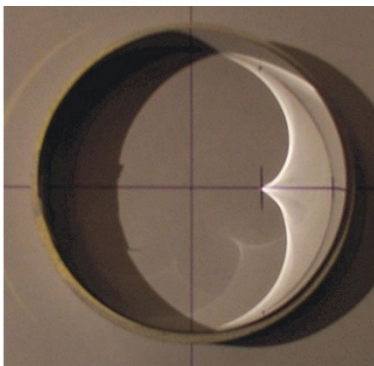


# Low Cost Physics Experiments using ITC *Salvador Gil*



$$E = mc^2$$



# Low Cost Physics Experiments using ITC

*S.Gil – Sept. 2022 -Preliminary Version*

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**To**

*Rodrigo, Eugenio, Mandy.  
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